2005

The 40th Anniversary of Fuzzy Sets

INFORMATION AND CONTROL 8, 338-353 (1965)

A New View an System Theory

Fuzzy Sets*

L. A. ZADEH

Department of Electrical Engineering and Electronics Research Laboratory, University of California, Berkeley, California

A fuzzy set is a class of objects with a continuum of grades of membership: Such a set is characterized by a membership (characteristic) function which assigns to each object a grade of membership ranging between zero and one. The notions of inclusion, union, intersection, complement, relation, convexity, etc., are extended to such sets, and various properties of these notions in the context of fuzzy sets are established. In particular, a separation theorem for convex fuzzy sets is proved without requiring that the fuzzy sets be disjoint.



Rudolf Seising Medical Statistics and Informatics Medical University of Vienna Vienna - Austria

History of the Theory of Fuzzy Sets

- Prehistory of the Theory of Fuzzy Sets 1920s-1960s
- Genesis of the Theory of Fuzzy Sets
 1960s
- Applications of the Theory of Fuzzy Sets 1970s
- Enforcement of the Theory of Fuzzy Sets as a scientific paradigm 1980s - 1990s



History of the Theory of Fuzzy Sets



History of the Theory of Fuzzy Sets

- Thinking Machines and Communication Systems: A New Field of Electrical Engineering
- System Theory: A New Scientific Discipline
- A New View on System Theory: Fuzzy Sets and Systems
- A short Outlook: The First Real World Application Fuzzy System



Lotfi Aliasker Zadeh



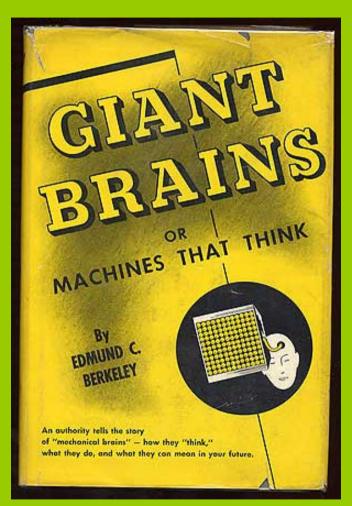






- born 1921 in Buku, Azerbaijan
- since 1942: Electrical Engineering, University Tehran
- then: Technical Associate of the US Army Forces in Iran
- 1944: Emigration into the USA, International Electronic Laboratories, New York Studies of Electrical Engineering at the MIT
- 1946: Master of Science, Supervisor: Robert Fano, Then: Columbia University, New York
- 1949: Ph. D. Thesis: *Frequency Analysis of Variable Networks* Supervisor: John Ralph Ragazzini
- 1950: An Extension of Wiener's Theory of Prediction (with Ragazzini)
- since 1952: Scientific Work: Information Theory and System Theory
- since 1964: Fuzzy Sets

Thinking Machines





Thinking Machines

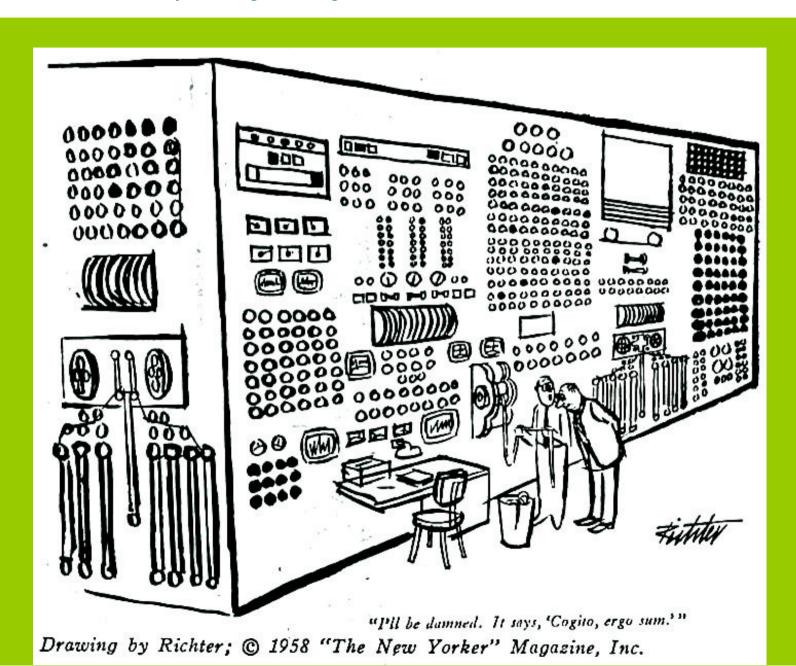
C. Diane Martin: The Myth of the Awesome Thinking Machine, *Communications of the ACM*, April 1993, Vol. 36, Nr. 4, pp. 120-133.

Characterization of ENIAC as a brain

Feb. 15, 1946:

"Army's New Wonder Brain and its Inventors."—Philadelphia Inquirer.
"Mathematical Brain Enlarges Man's Horizon."—Philadelphia Inquirer.
"Mechanical Mathematician 'Brain Child' of Hopkins Man."—The Baltimore Sun.
"Magic Brain Spurs Science and Technology."—New York World-Telegram.
"Electronic 'Brain' Computes 100-Year Problem in 2 Hours."—New York Herald Tribune.
"New 30-Ton Electronic 'Brain' Is Unveiled; Is World's Fastest Calculating Machine: Tubes Speed Up Laundryman's Abacus Principle."—The Evening Bulletin (Providence).
"Fastest Mechanical Brain Disclosed; Weighs 30 Tons: Giant Calculating Machine Said to Work 1,000 Times Faster Than Any Previously Built."—Chicago Sun.
"Computing Super-Brain Aids Army."—Newark Star Ledger.

I'll be damned. It says 'Cogito, ergo sum.'



UNIVAC (Universal Automatic Computer)

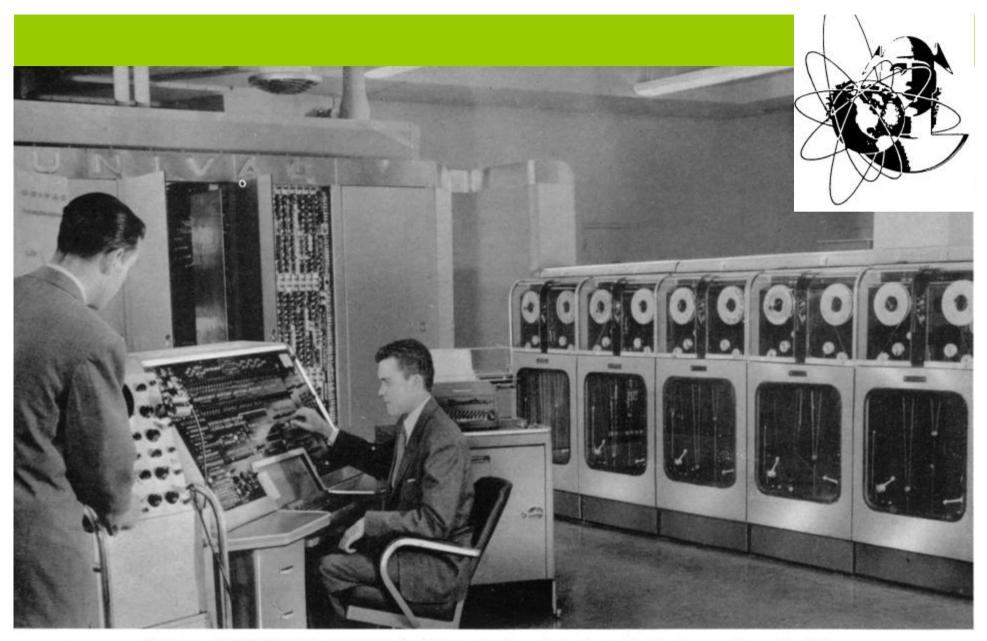
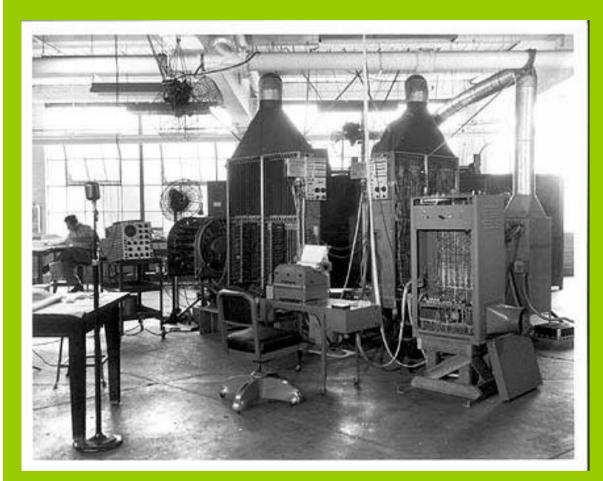


Plate 20. UNIVAC digital computer in the U.S.A., showing a bank of magnetic-tape storage units on the right

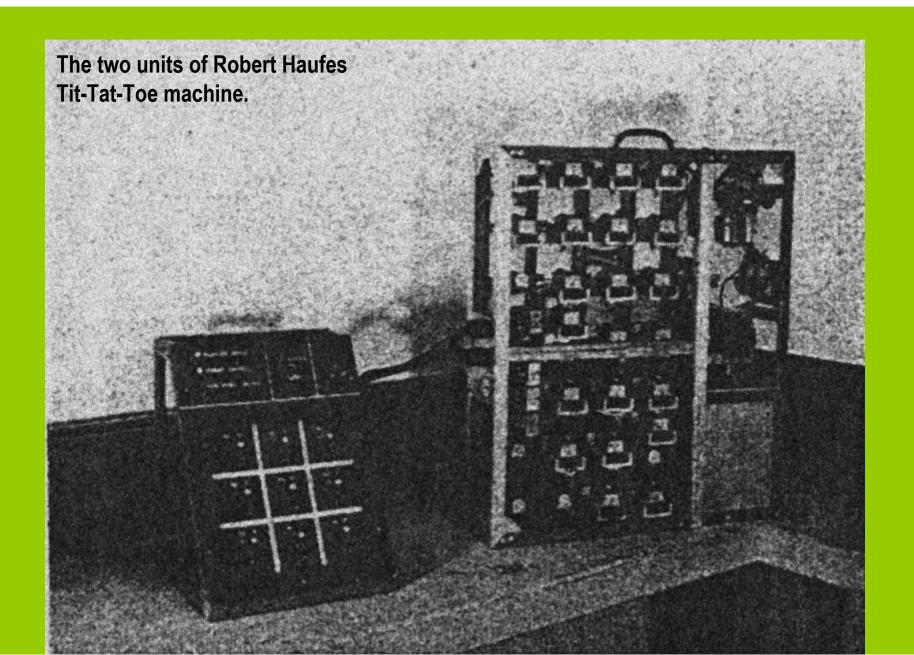
BINAC (Binary Automatic Computer)

BINAC was an early electronic computer designed for *Northorp Aircraft Company* by Eckert and Mauchly in 1949.

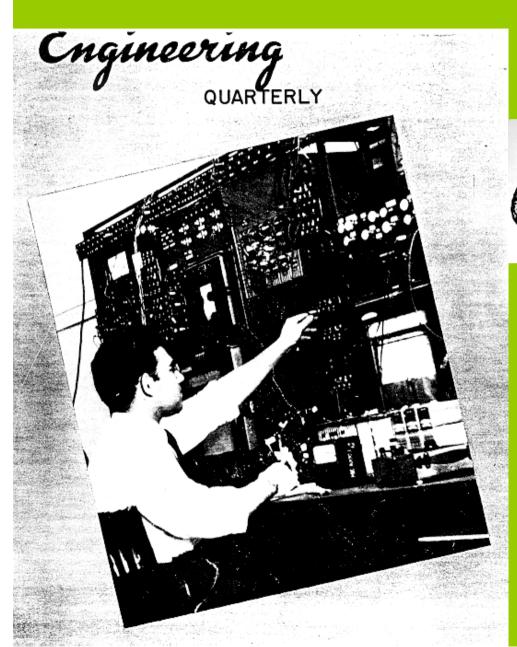


The BINAC was a bit-serial binary computer with two independent CPUs, each with its own 512-word acoustic mercury delay line memory. The CPUs continously compared results to check for errors caused by hardware failures. The 512-word acoustic mercury delay line memories were divided into 16 channels each holding 32 ords (31bit with an additional 11-bit space between words to allow for circuit delays in switching. The clock rate was 4.25 MHz which yielded a word time of about 10 microseconds. New programs or data had to be entered manually in octal using an eight-key keypad.

Lotfi A. Zadeh, 1950: Example of a "Thinking Machine"



Lotfi A. Zadeh, 1950: Thinking Machines, Columbia Engineering Quarterly, Jan. 1950.





THINKING MACHINES

A New Field in Electrical Engineering

> DR. LOFTI A. ZADEH ELECTRICAL ENGINEERING DEPT.



Lotfi A. Zadeh, 1950: Thinking Machines, Columbia Engineering Quarterly, Jan. 1950.

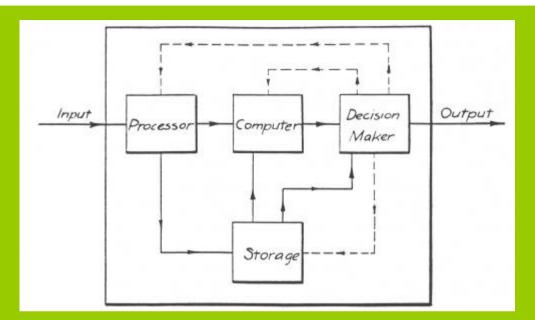
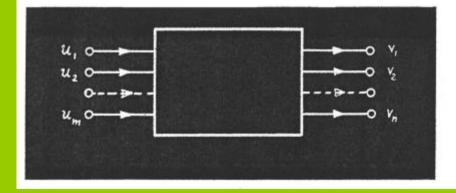


Figure 1—A schematic diagram illustrating how the basic elements of a thinking machine are arranged.

Relay Circuit Element	Symbolic Logic Interpretation
Circuit A	Statement A
Closed circuit	A is false
Open circuit	A is true
Series connection of A and B	A and/or B $(A \lor B)$
Parallel connection of A and B	A and B (A • B)

System Theory



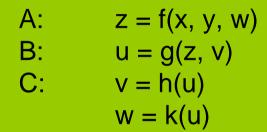
L. A. Zadeh

Associate Professor Electrical Engineering

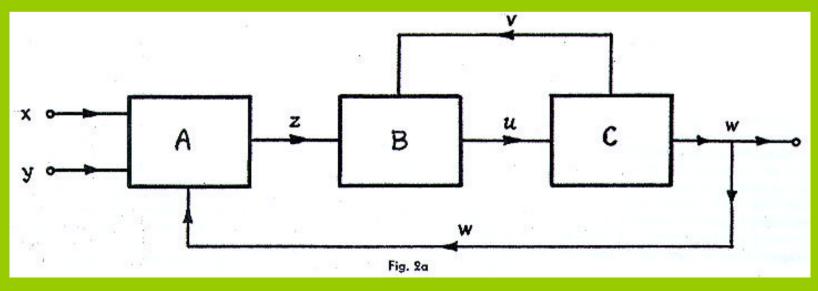
System:

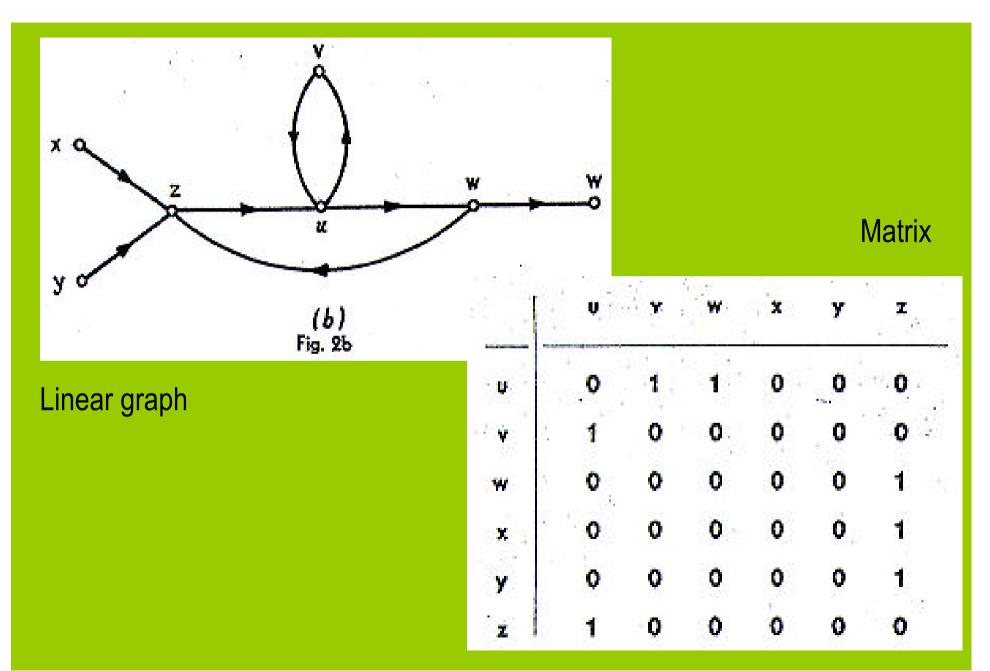
"an aggregation or assemblage of objects united by some form of interaction or interdependence"

(Webster's dictionary))



Block diagram





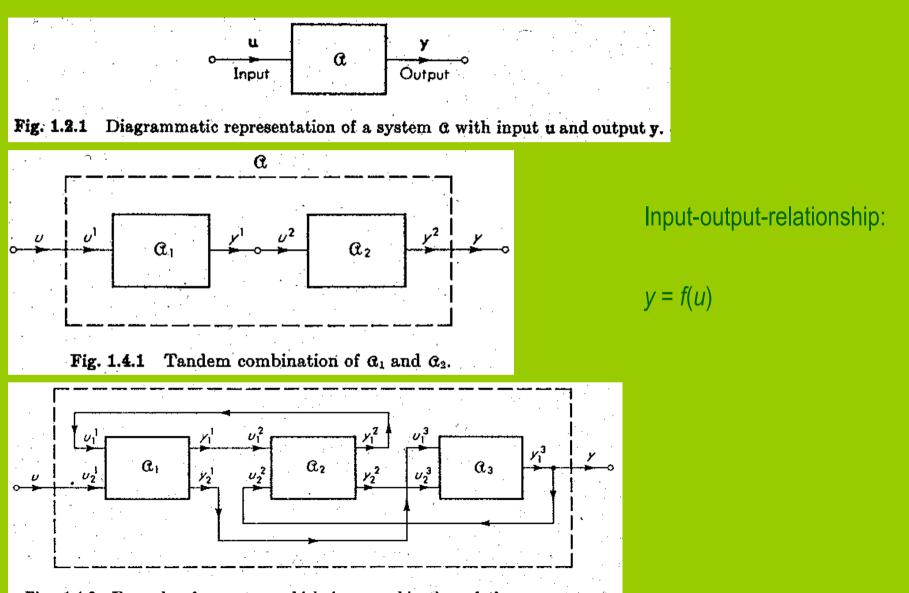


Fig. 1.4.2 Example of a system which is a combination of three component systems α_1 , α_2 , and α_3 .

The New York Academy of Sciences (1952) Series II, Vol. 14, No. 5, pp. 201-204.

Problem:

Let $X = \{x(t)\}$ be a set of signals. An arbitrarily selected member of this set, say x(t), is transmitted through a noisy channel **G** and is received as y(t).

As a result of the noise and distortion introduced by G, the received signal y(t) is, in general, quite different from x(t).

Nevertheless, under certain conditions it is possible to recover x(t) – or rather a timedelayed replica of it – from the received signal y(t).

 $y = G x \qquad resp. \qquad x = G^{-1} y$

The New York Academy of Sciences (1952) Series II, Vol. 14, No. 5, pp. 201-204.

Special case: reception process:

Let $X = \{x(t)\}$ consist of a finite number of discrete signals $x_1(t), x_2(t), ..., x_n(t)$, which play the roles of symbols or sequences of symbols.

The replicas of all these signals are assumed to be available at the receiving end of the system. Suppose that a transmitted signal x_k is received as y.

To recover the transmitted signal from y, the receiver evaluates the 'distance' between y and all possible transmitted signals $x_1, x_2, ..., x_n$, by the use of a suitable distance function d(x, y), and then selects that signal which is 'nearest' to y in terms of this distance function.

The New York Academy of Sciences (1952) Series II, Vol. 14, No. 5, pp. 201-204.

Distance functions:

- $d(x, y) = 1.u.b. \frac{1}{2x}(t) y(t)\frac{1}{2}$
- $d(x, y) = \{1/T \hat{\mathbf{Q}}^T[x(t) y(t)]^2 dt\}^{1/2}$
- $d(x, y) = \text{I.u.b.} \{1/T_0 \ \tilde{\mathbf{Q}}^{t+T}[x(t) y(t)]^2 \ dt \}^{1/2}$
- $d(x, y) = 1/T \dot{\mathbf{Q}}^{T_1/2x}(t) y(t)^{1/2}dt$

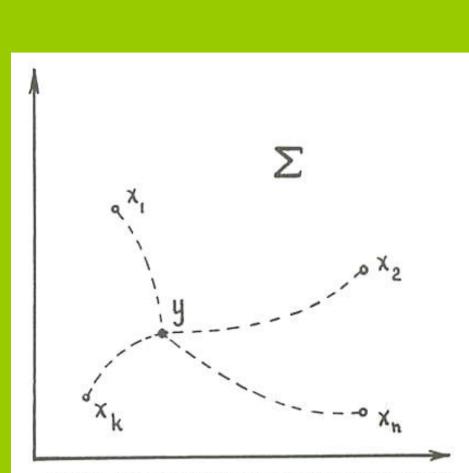


FIGURE 1. Recovery of the input signal by means of a comparison of the distances between the received signal y and all possible transmitted signals.

The New York Academy of Sciences (1952) Series II, Vol. 14, No. 5, pp. 201-204.

$d(x_k, y) < d(x_i, y)$ i ¹k, for all k and i.

3n many practical situations it is inconvenient, or even impossible, to define a quantitative measure, such as a distance function, of the disparity between two signals.

In such cases we may use instead the concept of neighbrhood, which is basic to the theory of topological spaces.'

The New York Academy of Sciences (1952) Series II, Vol. 14, No. 5, pp. 201-204.

Problem: multiplex transmission of two or more signals; the system has two channels.

 $X = \{x(t)\}$ and $Y = \{y(t)\}$: sets af signals assigned to their respective channels.

At the receiving end: sum signal: u(t) = x(t) + y(t).

To do: Extract x(t) and y(t) from u(t)!

That means:

Find two filters N_1 and N_2 such, that, for any x in X and any y in Y,

 $N_1(x + y) = x$ and $N_2(x + y) = y$

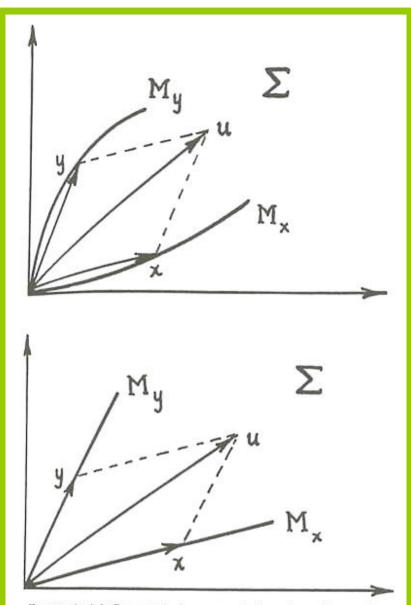


FIGURE 2. (a) Geometrical representation of nonlinear filtering. (b) Geometrical representation of linear filtering. The New York Academy of Sciences (1952) Series II, Vol. 14, No. 5, pp. 201-204.

Geometrical representation of

nonlinear filtering

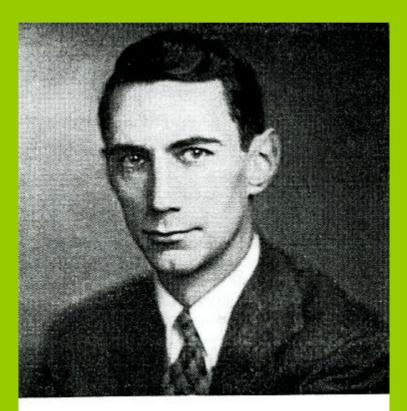
and

linear filtering

in terms of two-dimensional signal spaces.

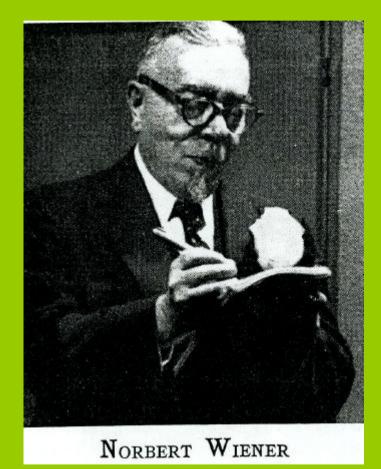
IRE Transactions on Information Theory, March/June1956

The Bandwagon



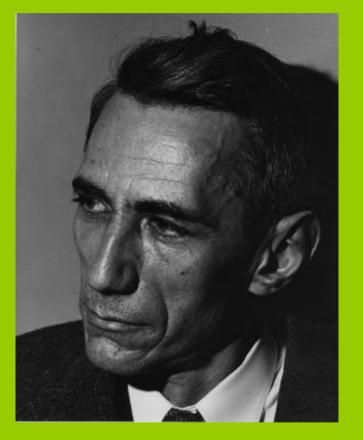
CLAUDE E. SHANNON

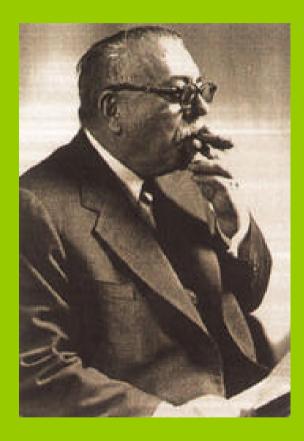
What is Information Theory?



Indeed, the hard core of information theory is, essentially, a branch of mathematics, a strictly deductive system.

Research rather than exposition is the keynote, and our critical thresholds should be raised.

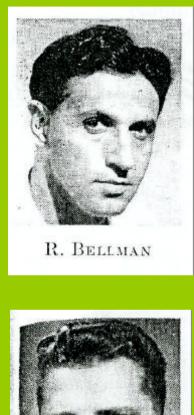


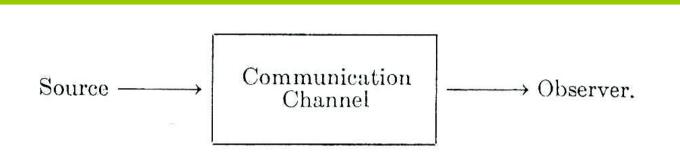


I am pleading in this editorial that Information Theory go back of its slogans and return to the point of view from which it originated: that of the general statistical concept of communication.

I hope that these Transactions may encourage this integrated view of communication theory by extending its hospitality to papers which, why they bear on communication theory, cross its boundaries, and have a scope covering the related statistical theories. In my opinion we are in a dangerous age of overspecialization.

Richard Bellman, Robert Kalaba, 1957: On the Role of Dynamic Programming in Statistical Communication Theory





In mathematical terms, let

- x = the pure signal emanating from S.
- r = the noise associated with the signal.
- x' = F(x, r), the input to the communication system. y = the signal transmitted to the observer by the
 - communication channel. (1)

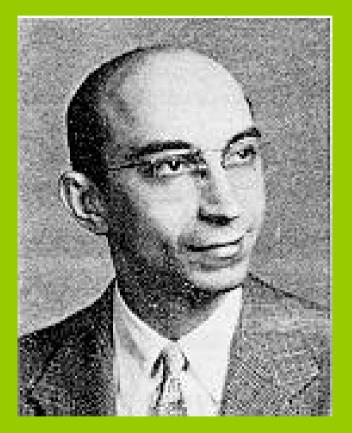
Let us further write

$$y = T(x') = T(F(x, r)),$$
 (2)

R. KALABA

IRE Transactions on Information Theory: March 1958

What Is Optimal?



Lotfi A. Zadeh

Criterion A:

- Design D_1 might be better than D_2 , and
- Design D_2 might be better than D_3 .

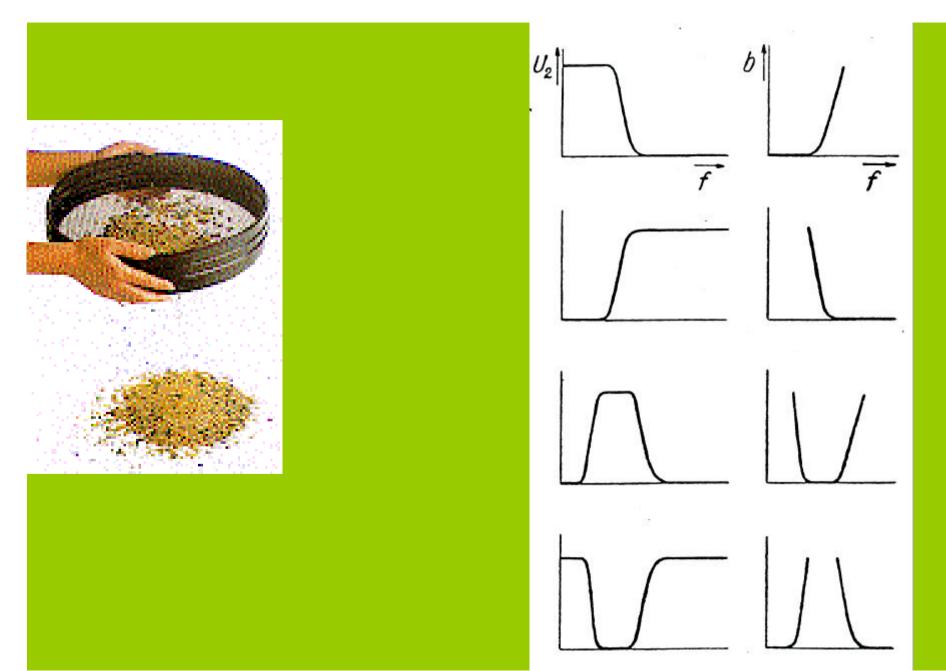
Criterion B:

- Design D_2 might be better than D_3 , and
- Design D_3 might be better than D_1 .

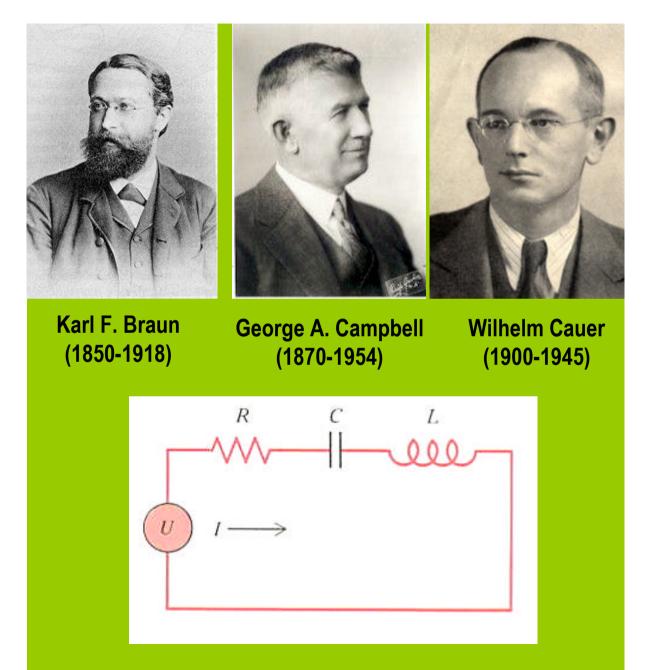
Criterion C:

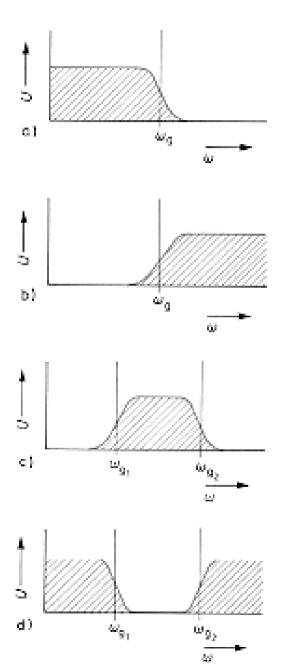
- Design D_3 might be better than D_1 , and
- Design D_1 might be better than D_2 .

Electrical Filters, Sieves



Electrical Filters, Sieves





Lotfi A. Zadeh: 1963, Linear System Theory

System with two variables v_1 and v_{2} ;

$$\frac{dv_2}{dt^2} = \frac{d^2v_1}{dt^2} + v_1$$

This system can be realized in different forms.

Lotfi A. Zadeh: 1963, Linear System Theory

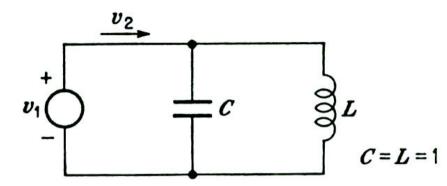


Fig. 1.4.1 A network realization of the object of Example 1.4.14.

Physical Realization 1:

elektrical network.

*v*₁: voltage

 v_2 : current.

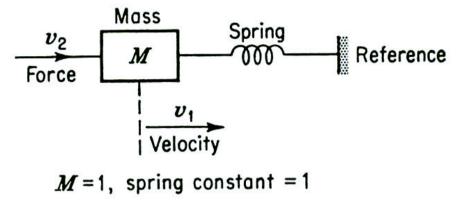
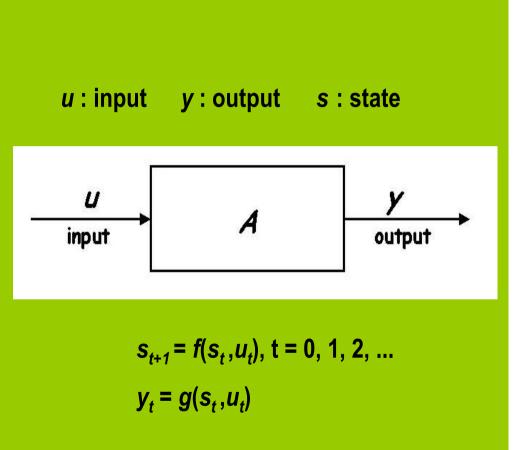


Fig. 1.4.2 A mechanical realization of the object of Example 1.4.14.

Phys mech v₂: fo v₁: ve

Physical Realization 2: mechanical system. v_2 : force at particle v_1 : velocity of the particle A System is a big black box Of which we can't unlock the locks, And all we can find out about Is what goes in and what goes out. Perceiving input-output pairs, Related by parameters, Permits us, sometimes, to relate An input, output, and a state. If this relation's good and stable Then to predict we may be able, But if this fails us – heaven forbid! We'll be compelled to force the lid!

Kenneth E. Boulding



Proceedings of The Second Systems Symposium

at Case Institute of Technology, April 1963, Cleveland, Ohio

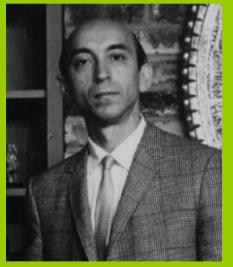
System Theory – The State Space Approach: A First New View on System Theory

Lotfi A. Zadeh, Charles A. Desoer: Linear System Theory, New York: McGraw-Hill 1963.

Lotfi A. Zadeh, Elijah Polak: System Theory, New York : McGraw-Hill, 1969.



Charles A. Desoer



Lotfi A. Zadeh



Elijah Polak

L. A. Zadeh, 1962: From Cercuit Theory to System Theory

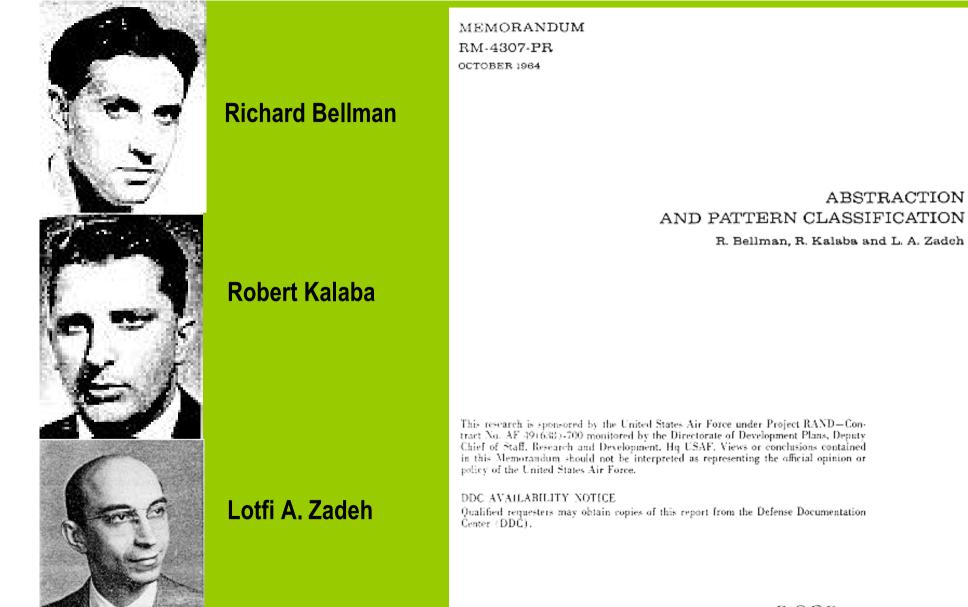
In: Proceedings of the IRE, May 1962, pp. 856-865.



In fact, there is a fairly wide gap between what might be regarded as "animate" system theorists and "inanimate" system theorists at the present time, and it is not at all certain that this gap will be narrowed, much less closed, in the near future.

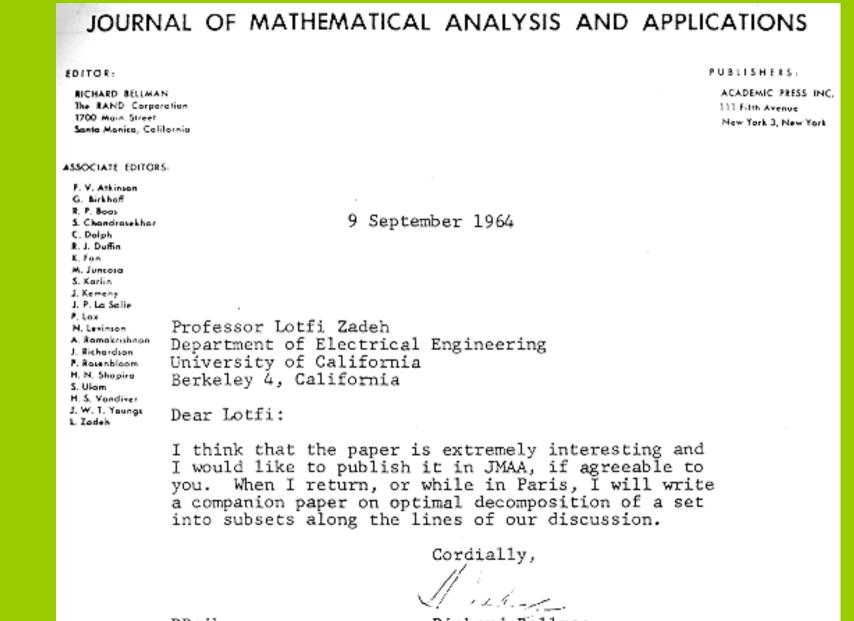
There are some who feel that this gap reflects the fundamental inadequacy of the conventional mathematics – the mathematics of precisely-defined points, functions, sets, probability measures, etc. - for coping with the analysis of biological systems, and that to deal effectively with such systems, which are generally orders of magnitude more complex than man-made systems, we need a radically different kind of mathematics, the mathematics of fuzzy or cloudy quantities which are not describable in terms of probability distributions. Indeed, the need for such mathematics is becoming increasingly apparent even in the realm of inanimate systems, for in most practical cases the a priori data as well as the criteria by which the performance of a manmade system is judged are far from being precisely specified or having accurately-known probability distributions.

R. Bellman, R. Kalaba, L. A. Zadeh, 1964: Abstraction And Pattern Classification





Letter: Bellman to Zadeh, September 9, 1964



RB:jb

Richard Bellman

Lotfi A. Zadeh, 1965: A New View of System Theory

Symposium on System Theory, April 20., 21. and 22. 1965, Polytechnic Institute, Brooklyn.

FUZZY SETS AND SYSTEMS*

L. A. Zadeh

Department of Electrical Engineering, University of California, Berkeley, California

The notion of fuzziness as defined in this paper relates to situations in which the source of imprecision is not a random variable or a stochastic process, but rather a class or classes which do not possess sharply defined boundaries, e.g., the "class of bald men," or the "class of numbers which are much greater than 10," or the "class of adaptive systems," etc.

A basic concept which makes it possible to treat fuzziness in a quantitative manner is that of a fuzzy set, that is, a class in which there may be grades of membership intermediate between full membership and non-membership. Thus, a fuzzy set is characterized by a membership function which assigns to each object its grade of membership (a number lying between 0 and 1) in the fuzzy set.

After a review of some of the relevant properties of fuzzy sets, the notions of a fuzzy system and a fuzzy class of systems are introduced and briefly analyzed. The paper closes with a section dealing with optimization under fuzzy constraints in which an approach to problems of this type is briefly sketched. $s_{t+1} = f(s_t, u_t),$ $y_t = g(s_t, u_t)$ t = 0, 1, 2, ...

S is a fuzzy system if u(t) or y(t) or s(t) or any combination are fuzzy sets.

Lotfi A. Zadeh, 1965: Fuzzy Sets

INFORMATION AND CONTROL 8, 338-353 (1965)

Fuzzy Sets*

L. A. ZADEH

Department of Electrical Engineering and Electronics Research Laboratory, University of California, Berkeley, California

A fuzzy set is a class of objects with a continuum of grades of membership. Such a set is characterized by a membership (characteristic) function which assigns to each object a grade of membership ranging between zero and one. The notions of inclusion, union, intersection, complement, relation, convexity, etc., are extended to such sets, and various properties of these notions in the context of fuzzy sets are established. In particular, a separation theorem for convex fuzzy sets is proved without requiring that the fuzzy sets be disjoint.

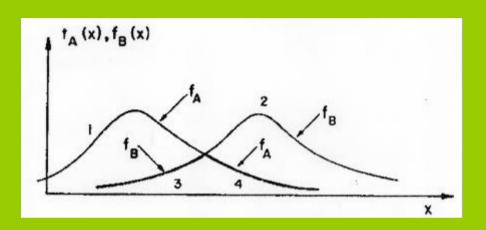
I. INTRODUCTION

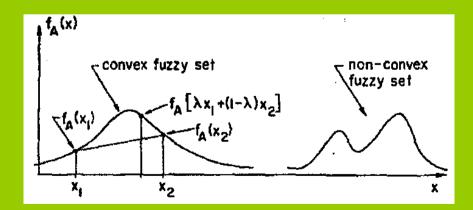
More often than not, the classes of objects encountered in the real physical world do not have precisely defined criteria of membership. For example, the class of animals clearly includes dogs, horses, birds, etc. as its members, and clearly excludes such objects as rocks, fluids, plants, etc. However, such objects as starfish, bacteria, etc. have an ambiguous status with respect to the class of animals. The same kind of ambiguity arises in the case of a number such as 10 in relation to the "class" of all real numbers which are much greater than 1.

Clearly, the "class of all real numbers which are much greater than 1," or "the class of beautiful women," or "the class of tall men," do not constitute classes or sets in the usual mathematical sense of these terms. Yet, the fact remains that such imprecisely defined "classes" play an important role in human thinking, particularly in the domains of pattern recognition, communication of information, and abstraction.

The purpose of this note is to explore in a preliminary way some of the basic properties and implications of a concept which may be of use in

* This work was supported in part by the Joint Services Electronics Program (U.S. Army, U.S. Navy and U.S. Air Force) under Grant No. AF-AFOSR-139-64 and by the National Science Foundation under Grant GP-2413.

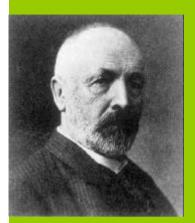




Georg Cantor, 1895/97: Set Theory



Georg Cantor, 1895/97: Set Theory

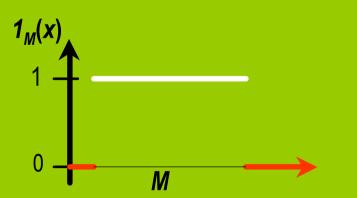


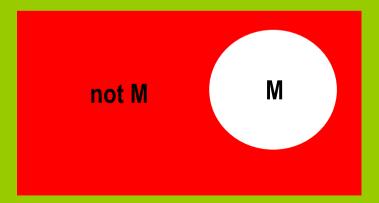
Georg Cantor (1845-1918):

Definition:

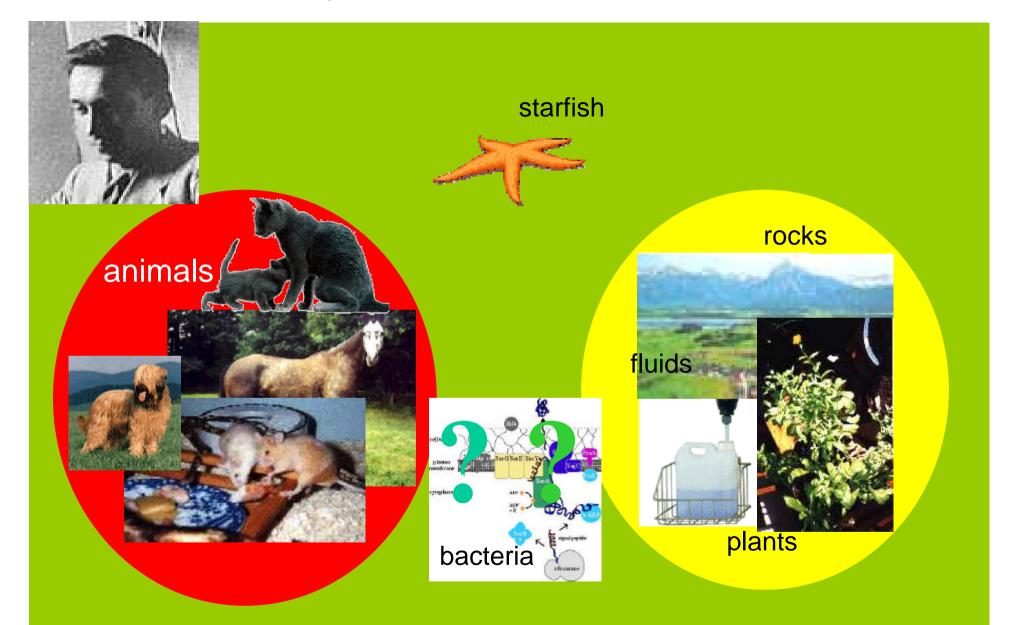
A set is a collection into a whole *M* of definite and separate objects *m* of our intuition or thought.'

"Unter einer Menge verstehen wir jede Zusammenfassung *M* von bestimmten, wohlunterschiedenen Objekten *m* unserer Anschauung oder unseres Denkens (welche die Elemente von *M* genannt werden) zu einem Ganzen."

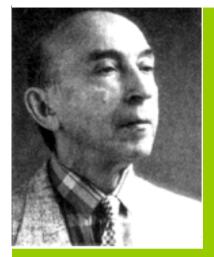




Lotfi A. Zadeh, 1965: Fuzzy Sets

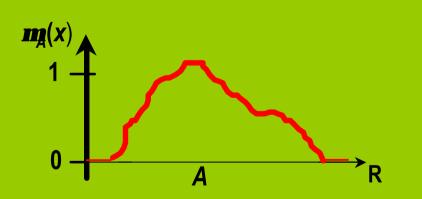


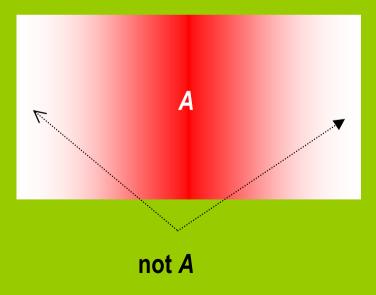
Lotfi A. Zadeh, 1965: Fuzzy Sets



Definition:

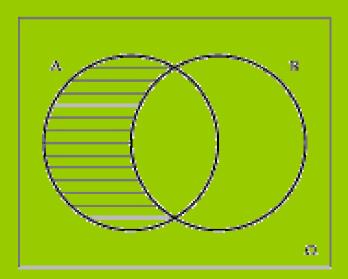
"A fuzzy set (class) A in X is characterized by a membership function (characteristic function) $\mathbf{m}_{\mathbf{X}}(x)$ which associates with each point in X a real number in the intervall [0,1], with the value of $\mathbf{m}_{\mathbf{X}}(x)$ at x representing the ,grade of membership' of x in A."



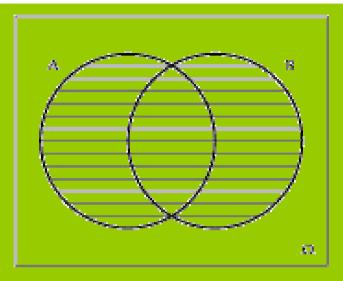


Set Theory

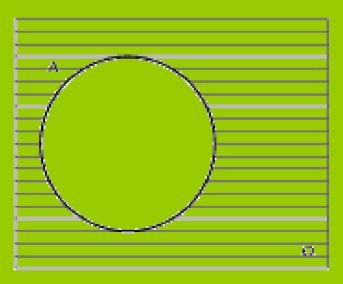
(a) A∩B







(b) A U B





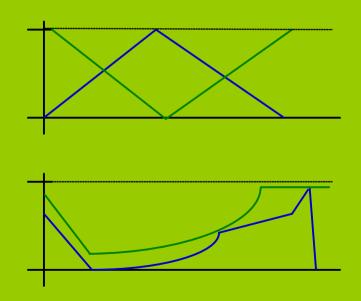
A fuzzy set is empty iff: $\mathbf{m}_A(x) = 0,$ $x \widehat{\mathbf{I}} X.$ Equal fuzzy sets, A = B, iff: $\mathbf{m}_A(x) = \mathbf{m}_B(x),$ $x \widehat{\mathbf{I}} X.$

The *complement A'* of a *fuzzy set A* is defined by:

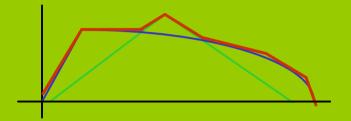
 $\mathbf{m}_{A'}(\mathbf{x}) = 1 - \mathbf{m}_{A'}(\mathbf{x}) \mathbf{x} \mathbf{\hat{I}} \mathbf{X}.$

Containment: A I B iff:

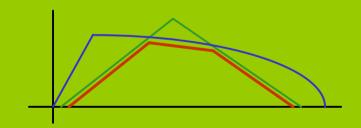
 $m_A(x) \leq m_B(x), \qquad x \in X.$



Union $A \stackrel{\frown}{E} B$ of two fuzzy sets A and B with resp. membership functions $m_{A \stackrel{\frown}{E} B}(x) = \max \{ m_A(x), m_B(x) \}, x \widehat{\mathbf{1}} X \}$

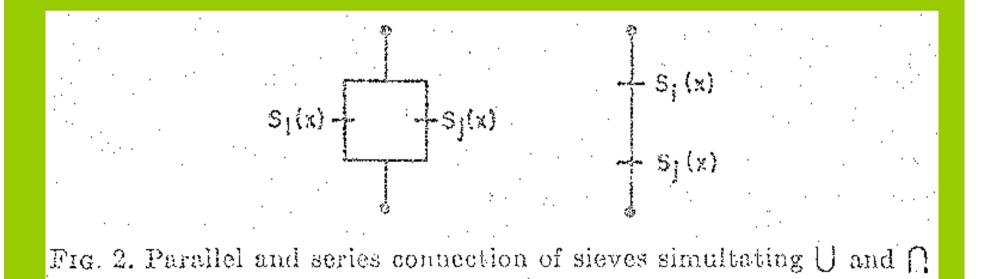


Intersection A \mathbf{C} B of fuzzy sets A and B with resp. membership functions $\mathbf{m}_{ACB}(\mathbf{X}) = \min \{\mathbf{m}_A(\mathbf{X}), \mathbf{m}_B(\mathbf{X})\}, \mathbf{X} \ \mathbf{\widehat{I}} \mathbf{X}$



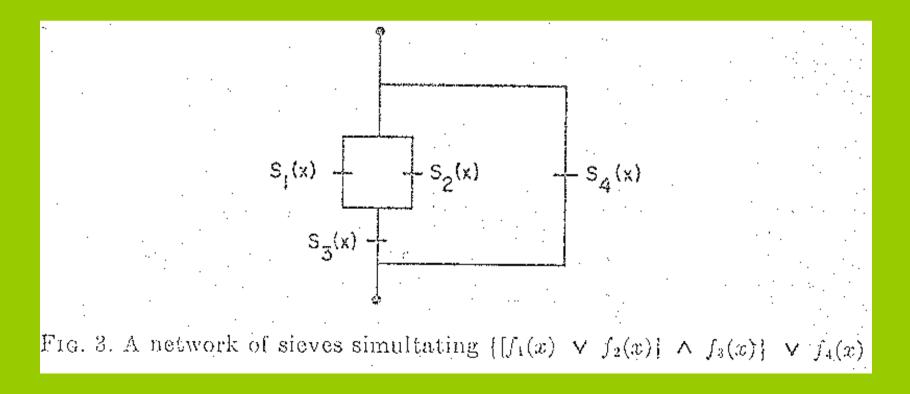
Lotfi A. Zadeh, 1965: Fuzzy Sets

"Specifically, let $f_i(x)$ i = 1, ..., n, denote the value of the membership function of A_i at x. Associate with $f_i(x)$ a sieve $S_i(x)$ whose meshes are of size $f_i(x)$. Then, $f_i(x) \stackrel{*}{\mathbf{E}} f_j(x)$ and $f_i(x) \stackrel{*}{\mathbf{C}} f_j(x)$ correspond, respectively, to parallel and series combinations of $S_i(x)$ and $S_i(x)$"



Lotfi A. Zadeh, 1965: Fuzzy Sets

"More generally, a well formed expression involving $A_1, ..., A_n$, È and Ç corresponds to a network of sieves $S_1(x), ..., S_n(x)$ which can be found by the conventional synthesis techniques for switching circuits."



First Ph. D Thesis on Fuzzy Sets

Fuzzy Sets and Pattern Recognition

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in the

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Categories of Furry Sets: Applications of Non-Cantarian Set Theory

8y

Joseph Amadee Coguen, Jr.

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First Papers on Fuzzy Sets (Part 1)

1965: L. A. Zadeh, Fuzzy Sets, *Information and Control*, 8, pp. 338-353

L. A. Zadeh, Fuzzy sets and systems. In: J. Fox Ed., *System Theory*. Microwave Research Institute Symp. Ser. XV. Brooklyn, NY: Polytechnic Press, pp. 29-37.

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- 1969: L. A. Zadeh, Biological applications of the theory of fuzzy sets and systems. In Proctor, L. D., Ed., *Biocybernetics of the Central Nervous System*. Boston, Mass.: Little, Brown & Co., 199-212.
- **1971:** L. A. Zadeh, Similarity relations and fuzzy orderings, *Inform. Sci.*, 3, pp. 177-200.

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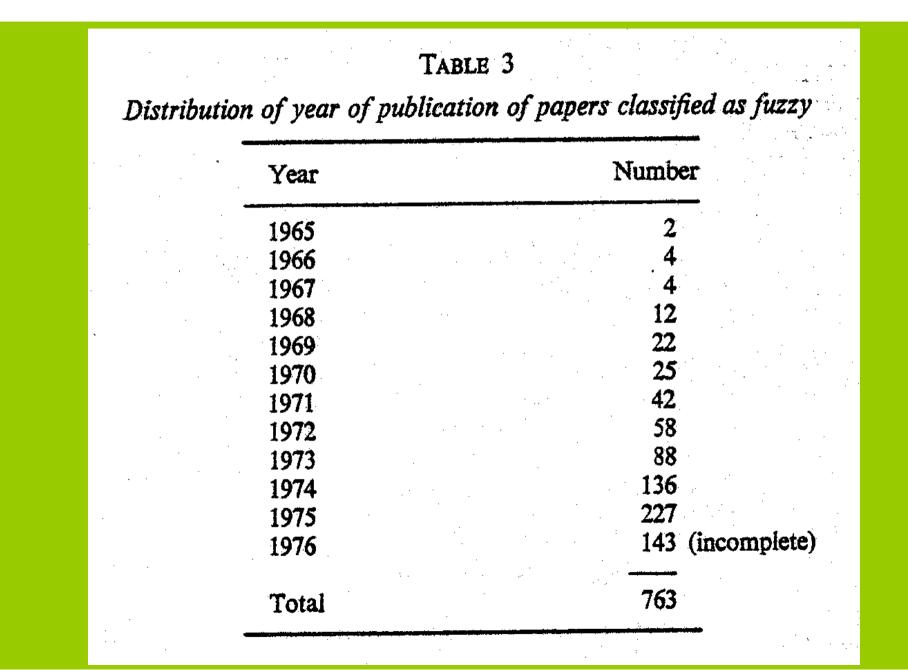
1972: L. A. Zadeh, Fuzzy languages and their relation to human intelligence. *Proceedings of the International Conference Man, And Computer*, Bordeaux, France. Basel: S. Karger pp. 130-165.

L. A. Zadeh, A new approach to system analysis. In: Marois, M. Ed., *Man and Computer*. Amsterdam: North Holland, pp. 55-94.

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- 1982: Lauritz P. Holmblad and Jens-Jørgen Østergaard: Control of a Cement Kiln by Fuzzy Logic. In: M. M. Gupta and E. Sanchez (eds.): *Fuzzy Information and Decision Processes*, North-Holland, 1982.

First Papers on Fuzzy Sets (Part 3)



First Papers on Fuzzy Sets (Part 4)

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The Berkeley Initiative in Soft Computing

BISC



Fuzzy Set: 1965 ... Fuzzy Logic: 1973 ... BISC: 1990 ... Human-Machine Perception: 2000 -

Statistics on the impact of fuzzy logic

A measure of the wide-ranging impact of Lotfi Zadeh's work on fuzzy logic is the number of papers in the literature which contain the word "fuzzy" in title. The data drawn from the INSPEC and Mathematical Reviews databases are summarized below. The data for 2000 are not complete.

STATISTICS

INSPEC/fuzzy 1970-1980 : 566 1980-1990 : 2,361 1990-2000 : 23,753 total: 26.680

Math.Sci.Net/fuzzy 1970-1980 : 453 1980-1990 : 2,476 1990-2000 : 8,428 total: 11,357

INSPEC/soft computing 1990-2000: 1,994

Number of citations in the Citation Index: over 11,000.

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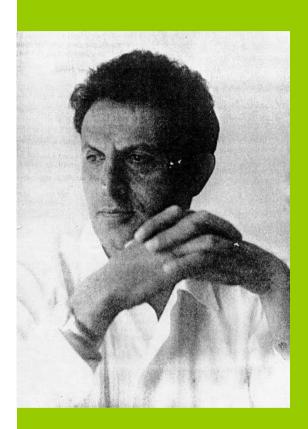
Professor Lotfi A. Zadeh

Short Curriculum Vitae Principal employment and affiliations Editorial affiliations Advisory committees Awards, fellowships, honors Achievement and principal contributions Summary of principal contributions Primary publications Statistics on the impact of Fuzzy Logic

Continue

Fuzzy Set: 1965 ... Fuzzy Logic: 1973 ... BISC: 1990 ... Human-Machine Perception: 2000 - ...

Richard Bellman, 1964

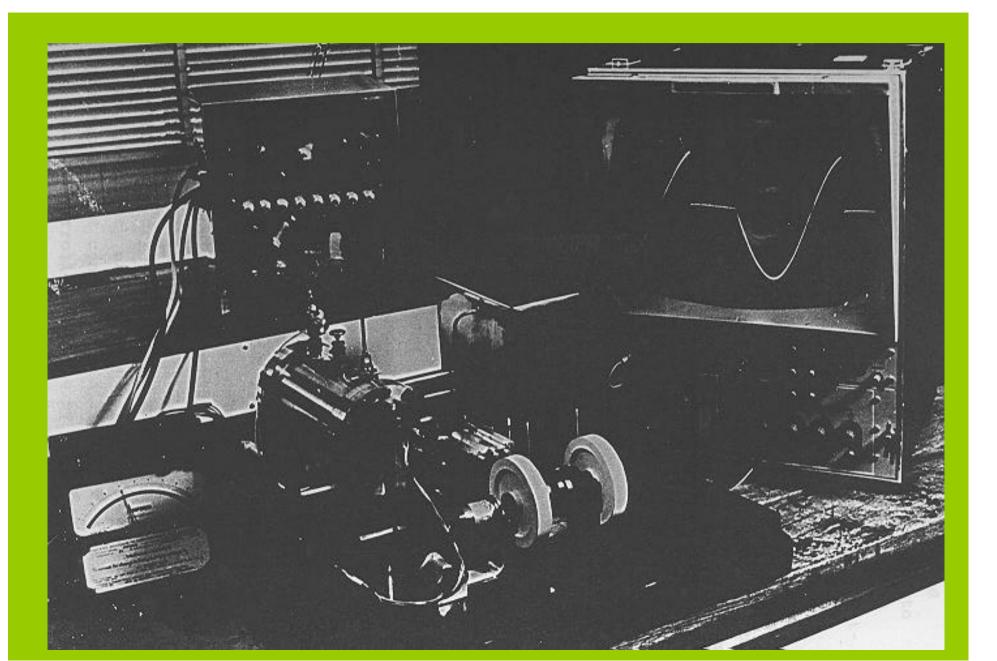


Man has two principal objectives in the scientific study of his environment:

He wants to understand and to control.

The two goals reinforce each other, since deeper understanding permits firmer control, and, on the other hand, systematic applications of scientific theories inevitably generates new problems which require further investigations, and so on.

Richard Bellman, Selected Papers on Mathematical Trends in Control Theory, New York: Dover 1964.



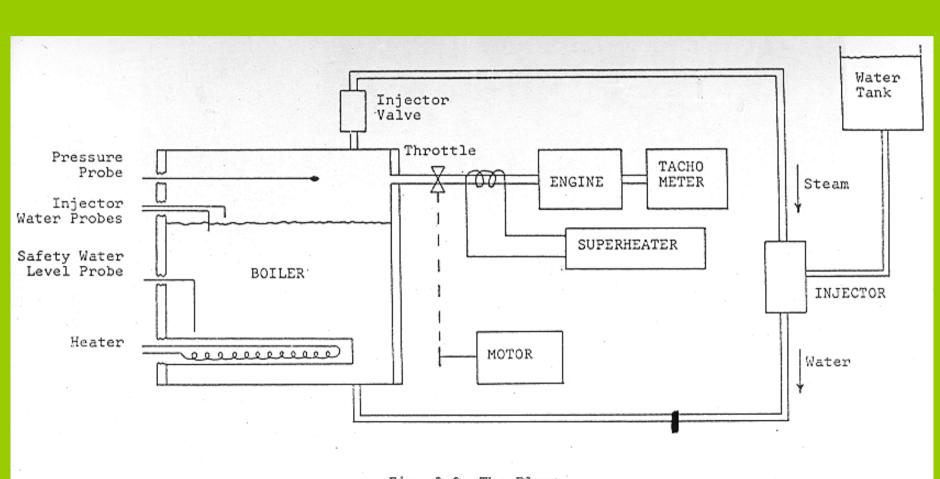
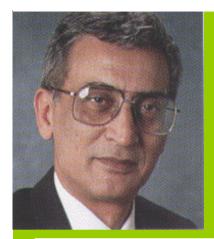


Fig. 2.2 The Plant

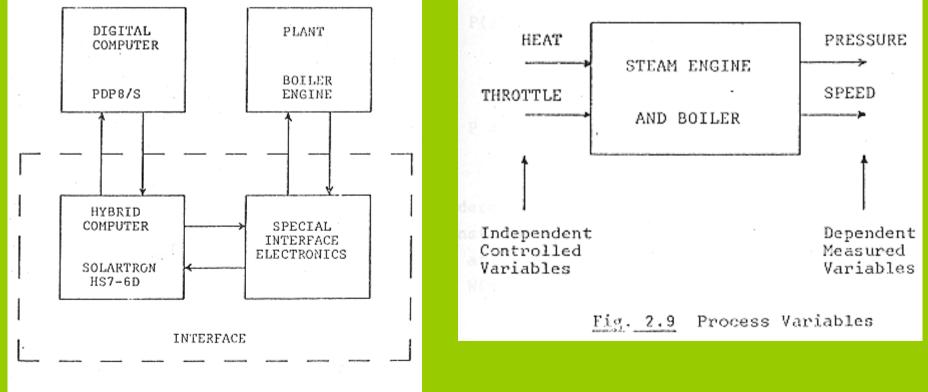
Fig. 2.1 The System



• Zadeh, 1973:

Outline of a New Approach to the Analysis of Complex Systems and Decision Processes

• Ebrahim H. Mamdani / Sedrak Assilian, 1974: "Fuzzy Steam Engine"



Assilian, Mamdani, 1974: An Experiment in Linguistic Synthesis with a Fuzzy Logic Controller

Fuzzy Control Variables

- PE Pressure Error
- CPE Change in pressure error
- HC Heat Change

Fuzzy Subsets

- PB Positive Big
- PM Positive Medium
- PS Positive Small
- NO Nil
- NS Negative Small
- NM Negative Medium
- NB Negative Big

Input variables:

Pressure Error

(Difference between tatsächlichem und vorgegebenem Druck.)

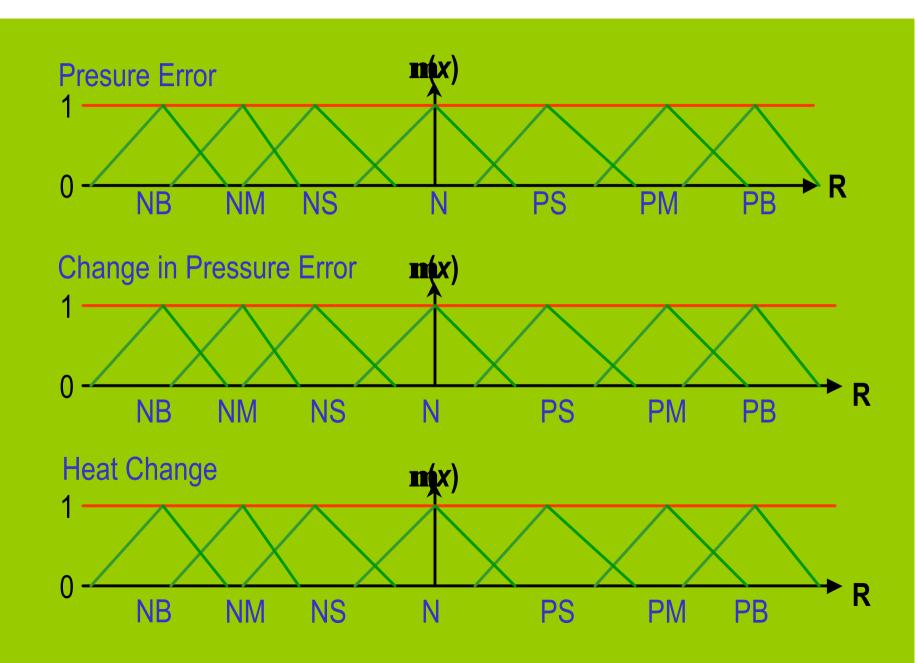
Change in Pressure Error

(Velocity of the movement oft the presureeschwindigkeit mit der sich der tatsächliche Druck

vom Sollwert entfernt bzw. nähert.)

Output variable:

•Heat Change



Regel 1:

WENN die *Druckabweichung* klein und positiv ist UND sich die *Druckabweichung* nicht viel ändert, DANN vermindere die *Wärmezufuhr* ein wenig.

WENN PK UND Null, DANN NK.

Regel 2:

WENN die Druckabweichung etwa Null ist UND sich die Druckabweichung nicht viel ändert, DANN verändere die Wärmezufuhr nicht.

WENN Null UND Null, DANN Null.

Regel 3:

WENN die *Druckabweichung* klein und positiv ist UND sich die *Druckabweichung* langsam vergrößert, DANN vermindere die *Wärmezufuhr* ein wenig.

WENN PK UND NK, DANN NK

Druckabweichung

		Negativ, groß	Negativ, mittel	Negativ, klein	Null	Positiv, klein	Positiv, mittel	Positiv, groß
		NG	NM	NK	Null	PK	РМ	PG
Änderung in der Druck- abweichung	NG				PG			
	NM			-	PM			
	NK				PK,	NK Regel 3	· · · · ·	•
	Null				Null Regel 2	NK Regel	NM	NG
	PK				NK			
	PM				NM			
	PG				NG			

